Higgs Couplings and Precision Electroweak Data

Brian Batell
University of Chicago

with Stefania Gori and Lian-Tao Wang arXiv:1209.6382

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Motivation

LHC experiments have discovered a new particle!

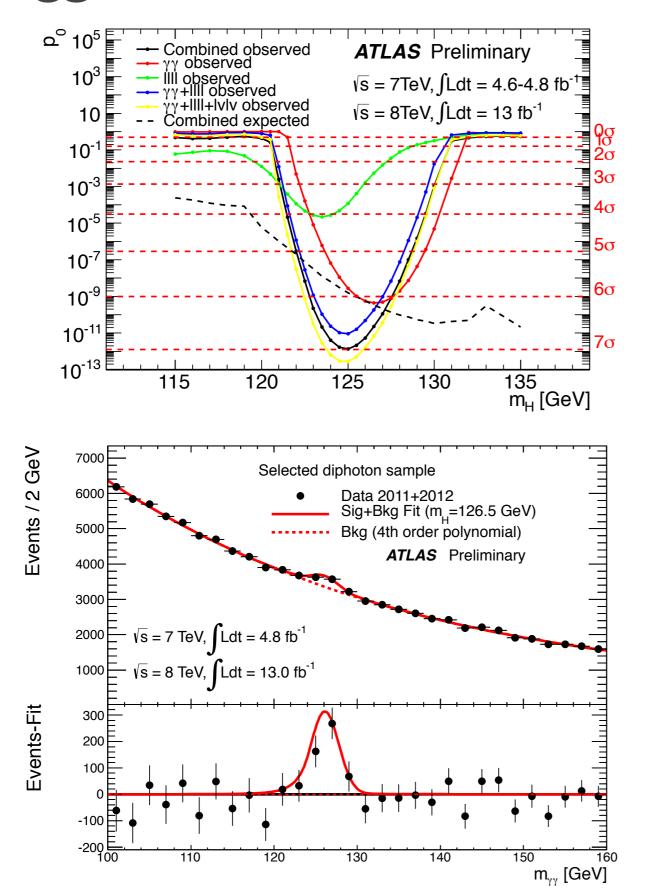
- Higgs-like state, mass ~ 126 GeV:
- Light, as suggested by precision electroweak data...
- Signal strength in diphoton channel a little high...
- But, statistics are low, certainly consistent with SM

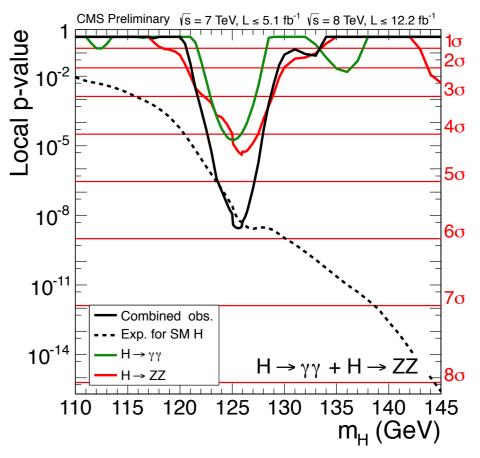
Precision Electroweak Data

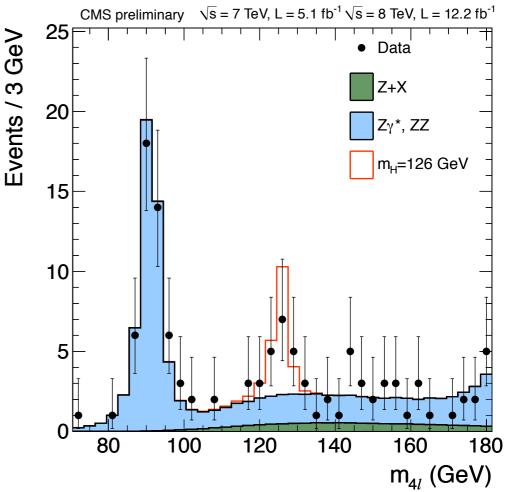
- Most observables are in agreement with SM predictions
- A persistent discrepancy: A_{FB}^b at Z-pole; (2.6σ)
- A new discrepancy (new theory calculation): R_b (2.4 σ)
- Tension with 126 GeV?

Let's explore the possible connections between Higgs physics and A_{FB}^b, R_b

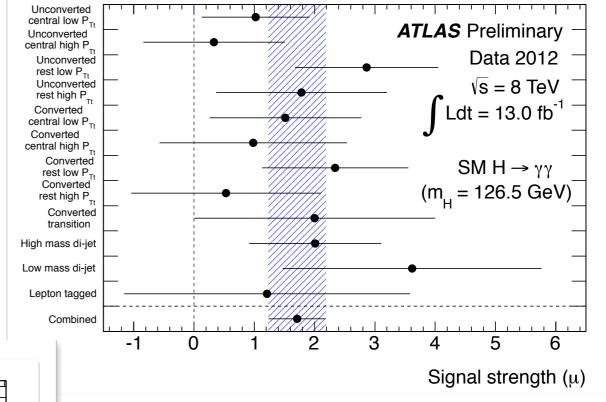
Higgs!

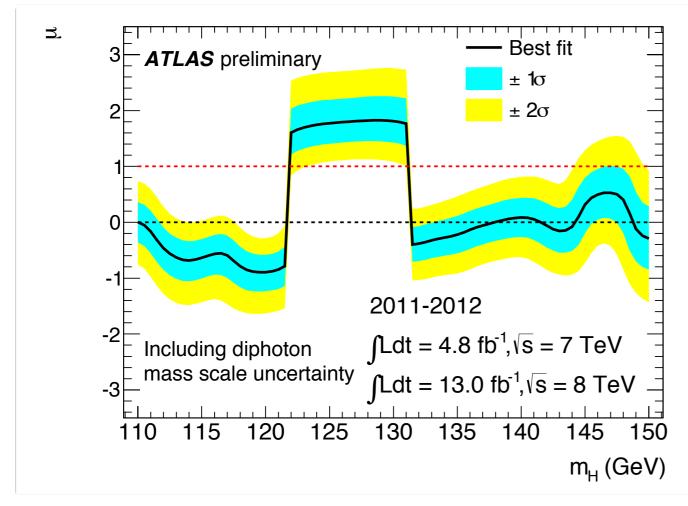




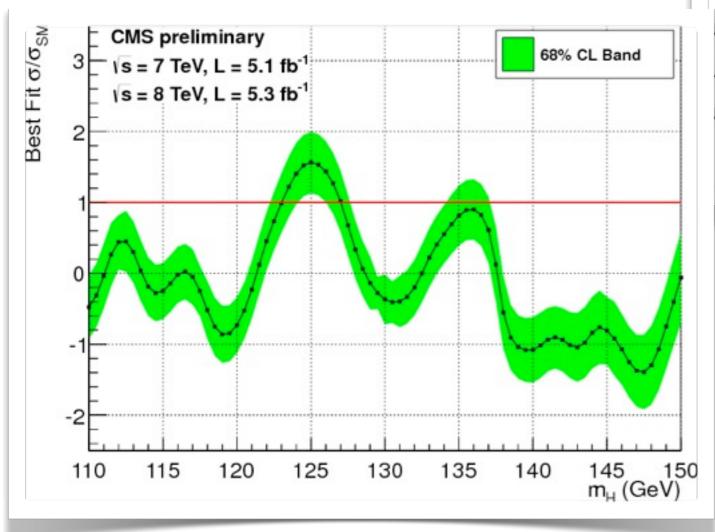


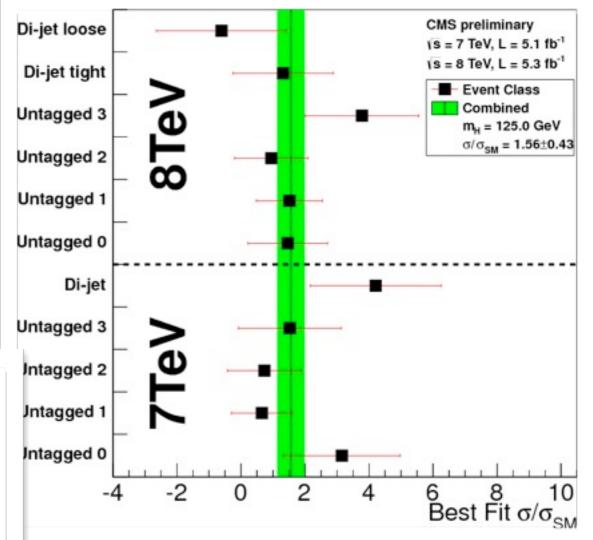
A few too many photons?





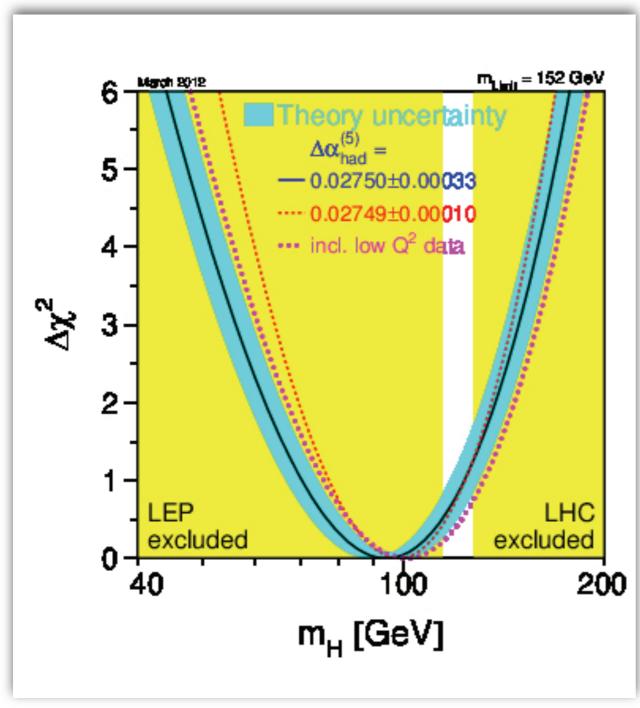
A few too many photons?





Note: CMS has not updated the diphoton analysis with the full dataset

Precision Electroweak Data (circa December 2011)



 $\sigma_{\mathsf{had}}^{\mathsf{0}}\left[\mathsf{nb}\right]$ 41.540 ± 0.037 41.478 20.767 ± 0.025 20.742 $0.01714 \pm 0.00095 \ 0.01646$ $A_{l}(P_{\tau})$ 0.1465 ± 0.0032 0.1482 $0.21629 \pm 0.00066 \ 0.21579$ 0.17220.1039 0.0992 ± 0.0016 0.0743 0.0707 ± 0.0035 0.923 ± 0.020 0.935 0.670 ± 0.027 0.668 0.1482 A_I(SLD) 0.1513 ± 0.0021 $\sin^2 \theta_{\rm eff}^{\rm lept}(Q_{\rm fb})$ 0.2324 ± 0.0012 0.2314 80.399 ± 0.023 m_w [GeV] 80.378 $\Gamma_{\mathsf{W}}\left[\mathsf{GeV}\right]$ 2.085 ± 0.042 2.092 m, [GeV] 173.20 ± 0.90 173.27 July 2011

Measurement

91.1875 ± 0.0021

 2.4952 ± 0.0023

 $0.02750 \pm 0.00033 \ 0.02759$

91.1874

2.4959

 $\Delta \alpha_{\rm had}^{(5)}({\rm m_7})$

m₇ [GeV]

 Γ_7 [GeV]

IO^{meas}–O^{fit}I/σ^{meas}

[LEP EWWG]

Global fits of the Standard Model

:
$$\chi^2/\text{dof} = 45/42$$
 (35%)

$$(35\%)$$

(Dec `12)

LEP EWWG (ZFitter):

$$\chi^2/{
m dof} = 17.3/13$$
 (19%) (Dec `I0)

$$\chi^2/{\rm dof} = 16.7/13$$
 (21%) (July `II)

http://gfitter.desy.de/

Since then:

1. Electroweak two loop

corrections for R_b [Freitas, Huang, 1205.0299]

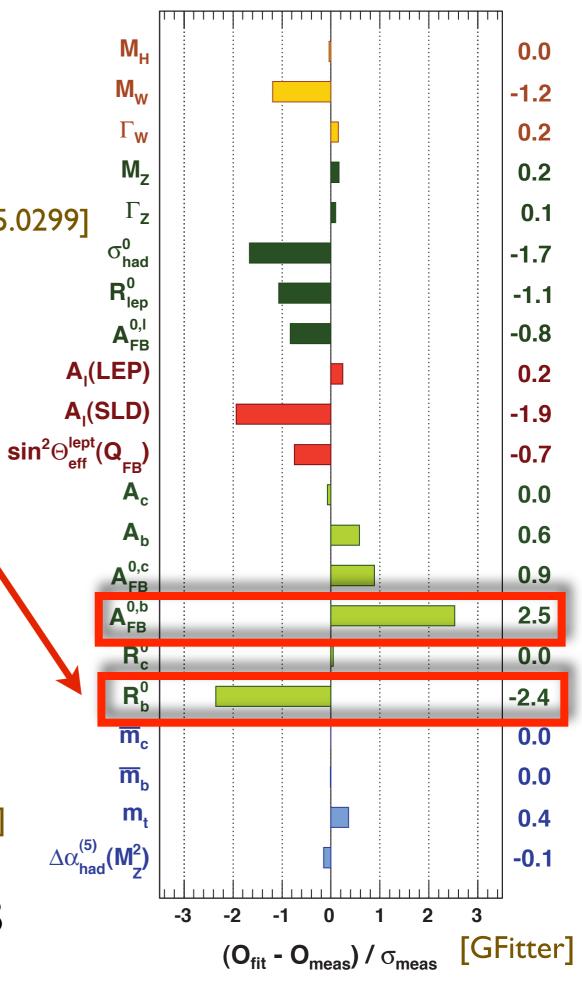
Now $> 2\sigma$ discrepancy!

2. Higgs discovered!

Higgs mass directly measured

Global fit (Gfitter): [arXiv:1209.2716]

$$\chi^2/\text{d.o.f.} = 21.8/14, \quad p = 0.08$$



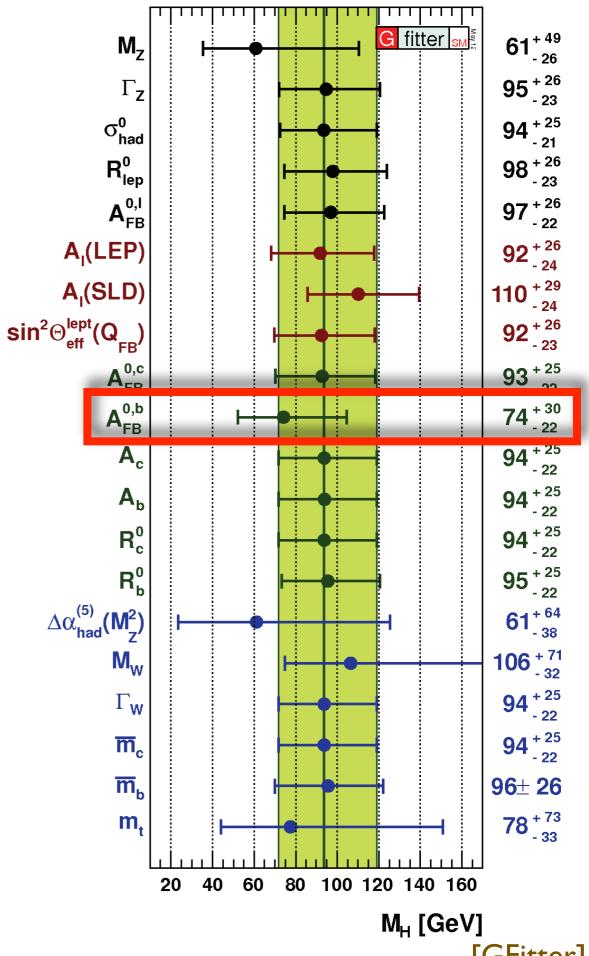
A puzzle?

Could very well be New Physics altering ${\cal A}^b_{FB}, {\cal R}_b$

However, $2-3\sigma$ discrepancies come and go all the time!

But ... if A_{FB}^b attributed to experimental error, electroweak fit prefers a very light Higgs, in tension with LEP bound

[Chanowitz '01]



[GFitter]

Can A_{FB}^b , R_b and $\gamma\gamma$ rate be due to same underlying new physics?

$$A_{FB}^{b}$$

$$\mathcal{L} \supset rac{g}{c_W} Z_\mu ar{b} (g_{Lb} P_L + g_{Rb} P_R) b$$

Consider the process

$$e^+e^- \to \gamma, Z, \to b\bar{b}$$

Forward, backward cross sections:

$$\sigma_{F,B} = \mp \int_0^{\pm 1} \frac{d\sigma}{d\cos\theta} d\cos\theta$$

Polarized cross sections:

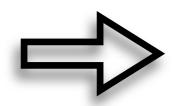
$$\sigma_{LL} \equiv \sigma(e_L^+ e_L^- \to b_L \bar{b}_L), \text{ etc.}$$

Forward-backward asymmetry:

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} \frac{\sigma_{LL} + \sigma_{RR} - \sigma_{LR} - \sigma_{RL}}{\sigma_{LL} + \sigma_{RR} + \sigma_{LR} + \sigma_{RL}}$$

On Z-pole:

$$\sigma_{LL} \propto rac{g_{Le}g_{Lb}}{m_Z\Gamma_Z}$$
 , etc.



$$A_{FB} = \frac{3}{4} \frac{g_{Le}^2 - g_{Re}^2}{g_{Le}^2 + g_{Re}^2} \frac{g_{Lb}^2 - g_{Rb}^2}{g_{Lb}^2 + g_{Rb}^2}$$

$$R_b$$

$$\mathcal{L} \supset rac{g}{c_W} Z_\mu \bar{b} (g_{Lb} P_L + g_{Rb} P_R) b$$

Z boson partial width: $\Gamma(Z o \psi_i ar{\psi}_i) \simeq rac{g^2}{24\pi c_W^2} (g_{Li}^2 + g_{Ri}^2) M_Z$

$$R_b \equiv \frac{\Gamma(Z \to b\bar{b})}{\Gamma(Z \to \text{hadrons})} \simeq \frac{g_{Lb}^2 + g_{Rb}^2}{\sum_q [g_{Lq}^2 + g_{Rq}^2]}$$

Note: both A_{FB}^b, R_b depend on couplings g_{Lb}, g_{Rb}

Suggests common resolution: tree-level shifts in $Zbar{b}$

Modify $Zb_R \overline{b}_R$ coupling

$$\mathcal{L} \supset \frac{g}{c_W} Z_{\mu} \bar{b} (g_{Lb} P_L + g_{Rb} P_R) b$$

$$g_{Lb} = -\frac{1}{2} + \frac{1}{3}s_w^2 \approx -0.43$$
$$g_{Rb} = \frac{1}{3}s_w^2 \approx 0.0771$$

Goal: shift A_{FB}^b and R_b

$$A_{FB} = \frac{3}{4} \frac{g_{Le}^2 - g_{Re}^2}{g_{Le}^2 + g_{Re}^2} \frac{g_{Lb}^2 - g_{Rb}^2}{g_{Lb}^2 + g_{Rb}^2} \qquad R_b \equiv \frac{\Gamma(Z \to b\bar{b})}{\Gamma(Z \to \text{hadrons})} \simeq \frac{g_{Lb}^2 + g_{Rb}^2}{\sum_q [g_{Lq}^2 + g_{Rq}^2]}$$

Z-pole data allows 4 solutions in $(\delta g_{Lb}, \delta g_{Rb})$, off-peak data for A_{FB}^b eliminate 2 possible solutions

Data prefers a bigger shift in δg_{Rb} , smaller shift in δg_{Lb}

Possible resolutions of A_{FB}^b , R_b discrepancies

- **1.** New physics directly alters A_{FB}^b, R_b
 - ullet Focus on tree level shifts to $Zbar{b}$ couplings

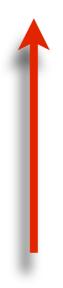
- **2.** A_{FB}^b, R_b due to measurement errors
 - Remove measurements from EW fit. Is there tension with 125 GeV Higgs?

How compelling are each of these resolutions?

To answer this question, we have performed a global fit to the precision electroweak data

Possible resolutions of A_{FB}^{b} , R_{b} discrepancies

- **1.** New physics directly alters A_{FB}^b, R_b
 - ullet Focus on tree level shifts to $Zbar{b}$ couplings



Focus on this possibility

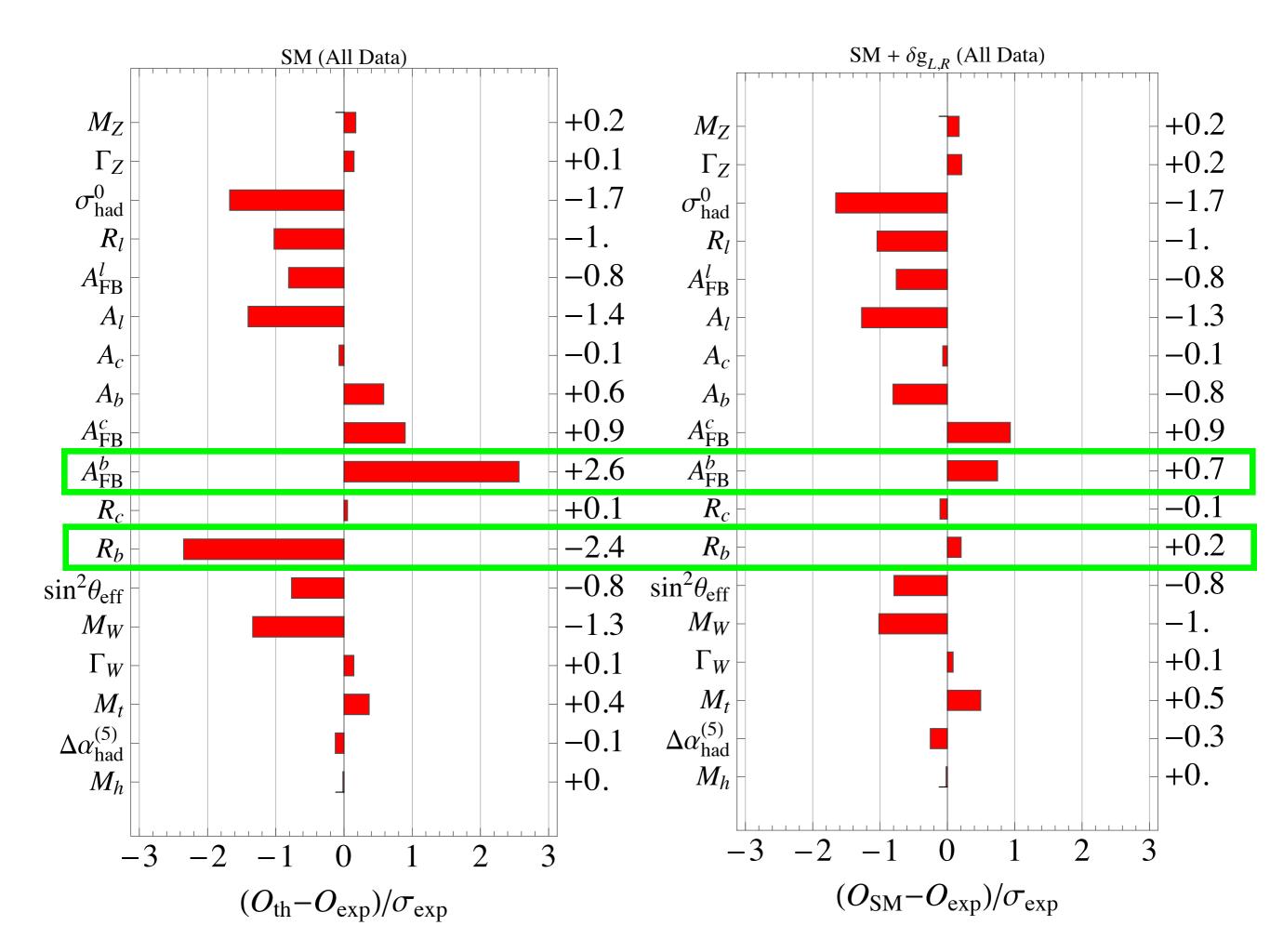
(more on 2nd option in backup)

New physics in A_{FB}^b , R_b ?

Standard Model:
$$\chi^2/\mathrm{d.o.f}=20.5/13, \quad p=0.08$$
 SM + $\delta g_{L,R}$: $\chi^2/\mathrm{d.o.f}=9.6/11, \quad p=0.57$

SM +
$$\delta g_{L,R}$$
: $\chi^2/\text{d.o.f} = 9.6/11, \quad p = 0.57$

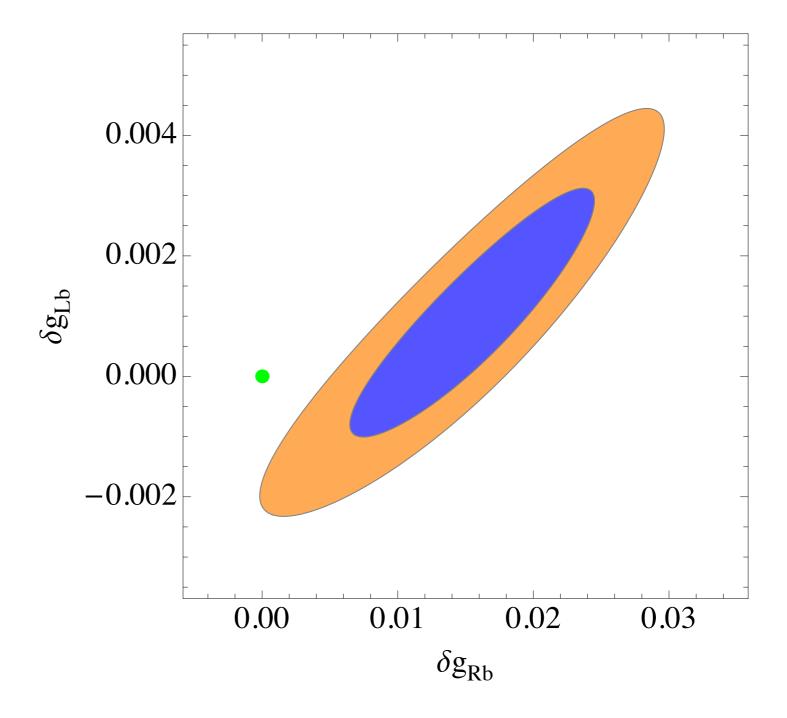
Fit with non-universal Zbb couplings much improved!



Best-fit region:

$$\delta g_{Lb} \sim 0.001 \pm 0.001$$

$$\delta g_{Rb} \sim 0.015 \pm 0.005$$



See also:

[Choudhury, Tait, Wagner '01] [Kumar, Shepard, Tait, Vega-Morales '10]

New physics models for A_{FB}^b, R_b

Beautiful Mirrors

[Choudhury, Tait, Wagner '01]

Basic idea: Mix new vector-like quark with bottom quark

$$\mathcal{L} \supset -\begin{pmatrix} \bar{b}'_L & \bar{B}'_L \end{pmatrix} \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix} \begin{pmatrix} b'_R \\ B'_R \end{pmatrix} + \text{h.c.}$$

Diagonalize mass matrix via rotations of $b_{i(L,R)}$, with angles $heta_{L,R}$

Z boson interactions:
$$\mathcal{L} \supset \frac{g}{c_w} Z_\mu \sum_{ij} \bar{b}_i \gamma^\mu (L_{ij} P_L + R_{ij} P_R) b_j$$

Shifts in Zbb couplings:

$$\delta g_{Lb} = \left(t_{3L} + \frac{1}{2}\right) s_L^2, \qquad \delta g_{Rb} = t_{3R} s_R^2,$$

Singles out 3 vector-like representations:

$$\Psi_{L,R} \sim (3,2,1/6), (3,2,-5/6), (3,3,2/3)$$

Focus on
$$\Psi \sim (3,2,-5/6) \sim \left(\begin{array}{c} B \\ X \end{array}\right)$$

$$Q_X = -4/3$$

$$t_{3R}^B = \frac{1}{2}$$
 $\delta g_{Rb} = \frac{1}{2} s_R^2 = 0.015$ $s_R \sim 0.17$ (small mixing)

Minimal model:

$$-\mathcal{L} \supset y_1 \bar{Q} H b_R + y_2 \bar{\Psi}_L H^{\dagger} b_R + M \bar{\Psi}_L \Psi_R + \text{h.c.} .$$

$$= (\bar{b}_L B_L) \left[\begin{pmatrix} Y_1 & 0 \\ Y_2 & M \end{pmatrix} + \frac{h}{v} \begin{pmatrix} Y_1 & 0 \\ Y_2 & 0 \end{pmatrix} \right] \begin{pmatrix} b_R \\ B_R \end{pmatrix}, \quad Y_i \equiv \frac{y_i v}{\sqrt{2}}$$

shifts:
$$\delta g_{Rb} \simeq \frac{Y_2^2}{2M^2} \quad \Longrightarrow \quad Y_2 \sim 0.17M$$

- Small oblique parameters S,T [Peskin, Takeuchi '90, '92]
- Light Higgs, heavy mirror quarks preferred by EW data

Higgs physics

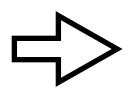
Main effects in Higgs production and decay:

- 1. Rotations shift in the $hb\bar{b}$ vertex: $\mathcal{L}_{hbb}\simeq -c_R^2\frac{m_b}{v}h\bar{b}b$ Partial width $h\to b\bar{b}$ suppressed by c_R^4
- **2.** Heavy quark B contributes to $h \to gg$ and $h \to \gamma\gamma$

can be characterized in terms of ratios

$$r_b, r_g, r_\gamma, ~~ r_i \equiv rac{\Gamma(h
ightarrow i)}{\Gamma(h
ightarrow i)_{
m SM}}$$

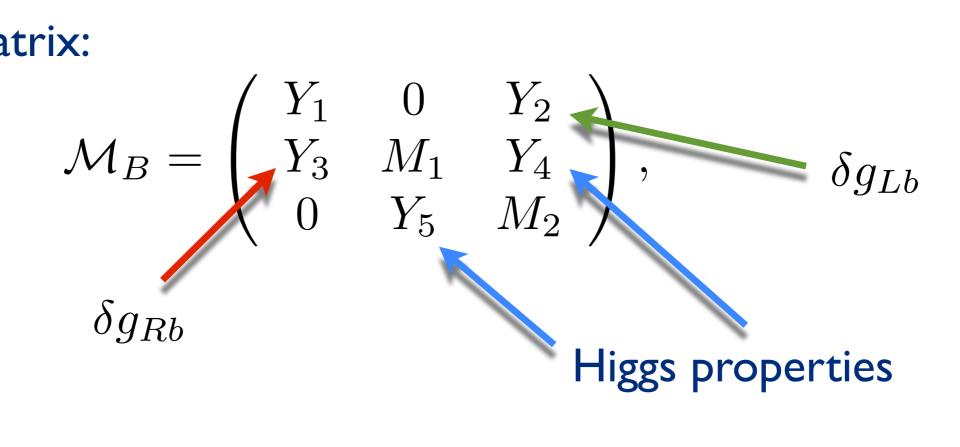
But, mixing angle and Yukawas are small in the minimal model



Higgs boson is SM-like (10% shifts at most)

Extension of the minimal model:

- One can further improve the EW fit by adding an SU(2) singlet quark $\hat{B} \sim (3,1,-1/3)$ that mixes with the bottom
- This causes a shift $\delta g_{Lb} \sim 0.001$
- Mass matrix:



• Large Y_4, Y_5 can alter Higgs rates, but also cause large custodial symmetry breaking; \longrightarrow custodial extension

A custodial extension:

SM quantum numbers:

$$\Psi_{L,R}^T = (B, X) \sim (3, 2, -5/6),$$

 $\hat{B}_{L,R} \sim (3, 1, -1/3),$
 $\hat{X}_{L,R} \sim (3, 1, -4/3).$

• Quantum numbers under $SU(2)_L \times SU(2)_R \times U(1)_X$

$$\Psi_{L,R}^T = (B, X) \sim (2, 1)_{-5/6}$$

 $\hat{\Psi}_{L,R}^T = (\hat{B}, \hat{X}) \sim (1, 2)_{-5/6}$

 Such representations can find motivation in composite Higgs models
 [Agashe, Contino, Da Rold, Pomarol '06]

Lagrangian

$$-\mathcal{L} \supset M_{1}\bar{\Psi}'_{L}\Psi'_{R} + M_{2}\hat{B}'_{L}\hat{B}'_{R} + M_{3}\hat{X}'_{L}\hat{X}'_{R} + y_{1}\bar{Q}'_{L}Hb'_{R} + y_{2}\bar{Q}'_{L}H\hat{B}'_{R} + y_{3}\bar{\Psi}'_{L}\tilde{H}b'_{R} + y_{4}\bar{\Psi}'_{L}\tilde{H}\hat{B}'_{R} + y_{5}\bar{B}'_{L}\tilde{H}^{\dagger}\Psi'_{R} + y_{6}\bar{\Psi}'_{L}H\hat{X}'_{R} + y_{7}\bar{X}'_{L}H^{\dagger}\Psi'_{R}$$

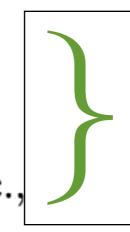
- Custodial limit: $M_2 = M_3, \ y_4 = y_6, \ y_5 = y_7$
- Note that y_1 , y_2 , y_3 explicitly break custodial symmetry, but only small values required to obtain required shifts δg_{Lb} , δg_{Rb} ,

Collider bounds on heavy quarks suggest $Y_i \ll M_{1.2.3}$

Integrate out heavy fermions to obtain effective theory

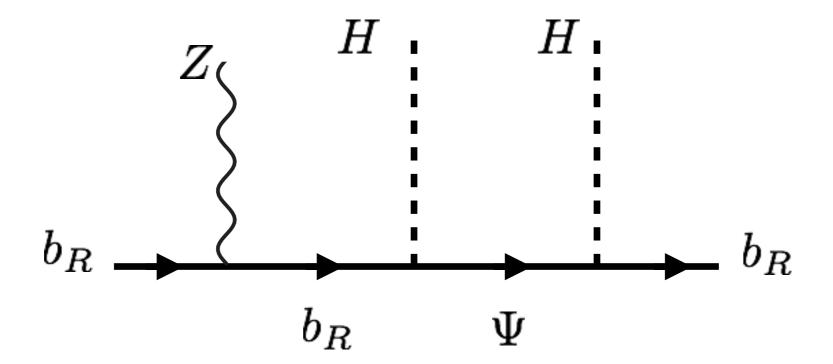
$$\mathcal{L} = \sum_i a_i \mathcal{O}_i$$

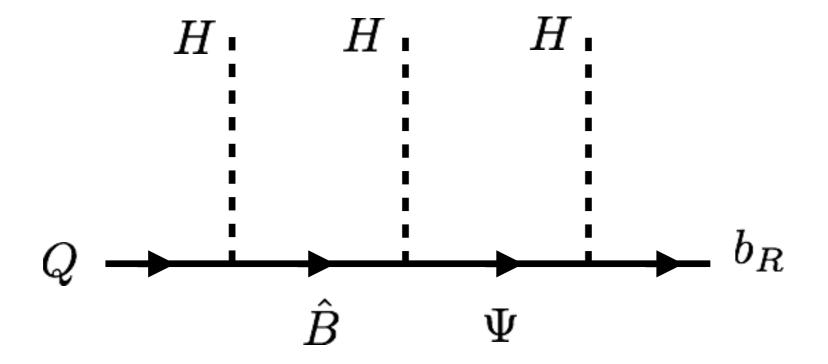
$$\begin{split} \mathcal{O}_{Hb} &= i(H^\dagger D_\mu H)(\bar{b}_R \gamma^\mu b_R) + \text{h.c.}, \\ \mathcal{O}_{HQ}^s &= i(H^\dagger D_\mu H)(\bar{Q} \gamma^\mu Q) + \text{h.c.}, \\ \mathcal{O}_{HQ}^t &= i(H^\dagger \sigma^a D_\mu H)(\bar{Q} \gamma^\mu \sigma^a Q) + \text{h.c.}, \end{split}$$
 lead to shift in $\delta g_{Lb}, \ \delta g_{Rb}, \ \delta g_{Rb}, \end{split}$



$$\mathcal{O}_{HY} = (H^\dagger H)(ar{Q}Hb_R) + ext{h.c..}$$
 $\Big\}$ lead to shift in $m_b, y_{hbar{b}}$







Non-universal
$$Zbar{b}$$
 shifts: $\delta g_{Lb}=rac{Y_2^2}{2M_2^2}, \quad \delta g_{Rb}=rac{Y_3^2}{2M_1^2}$

Recall $\delta g_{Rb} \sim 0.015$, $\delta g_{Lb} \sim 0.001$,

$$Y_2 \simeq \pm 0.04 \, M_2 \quad Y_3 \simeq \pm 0.17 \, M_1$$

$$b$$
 - quark mass & $m_b = Y_1 \left(1 - rac{Y_2^2}{2M_2^2} - rac{Y_3^2}{2M_1^2}
ight) + rac{Y_2Y_3Y_5}{M_1M_2} \ h - b - ar{b} \;\; ext{coupling} \qquad y_{hbb} = rac{1}{v} \left[Y_1 \left(1 - rac{3Y_2^2}{2M_2^2} - rac{3Y_3^2}{2M_1^2}
ight) + rac{3Y_2Y_3Y_5}{M_1M_2}
ight]$

$$r_b = \left(\frac{y_{hbb}}{m_b/v}\right)^2 \approx 1 + 8\sqrt{\delta g_{Rb}\delta g_{Rb}} \frac{Y_5}{m_b}$$

Large corrections to h o bar b possible only if Y_5 large

h o gg and $h o \gamma\gamma$: Use low energy theorem

[Ellis, Gaillard, Nanopoulos `76] [Shifman, Vainshtein, Voloshin, Zakharov `79]

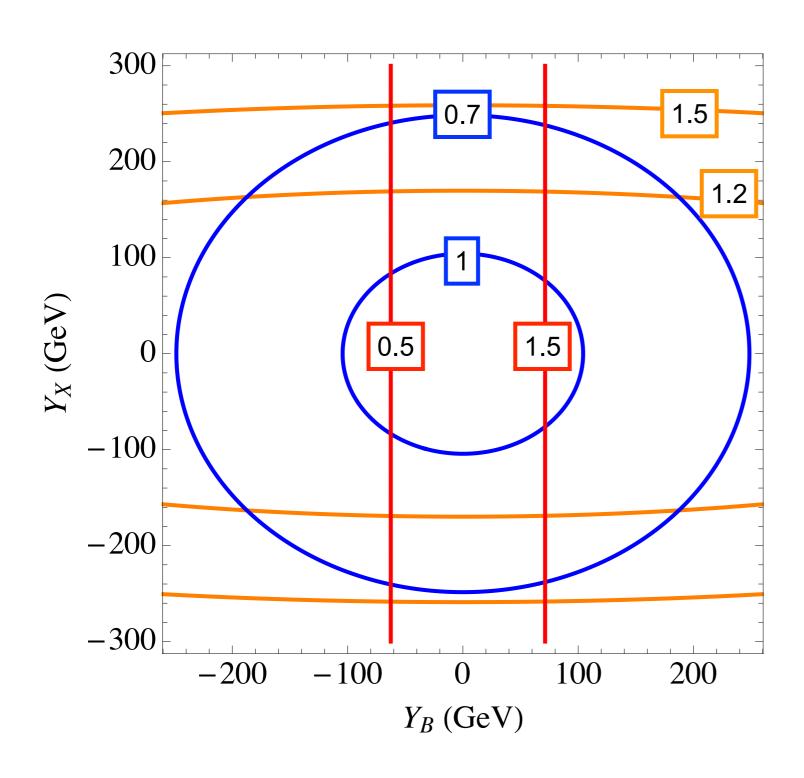
$$\mathcal{L} \supset rac{lpha}{16\pi v} \left[\sum_{f=B,X} b_f^{EM} z_f \,
ight] h F_{\mu
u} F^{\mu
u} + rac{lpha_s}{16\pi v} \left[\sum_{f=B,X} b_f^c z_f \,
ight] h G^a_{\mu
u} G^{\mu
u a},$$

$$b_B^{EM} = 4/9, \quad b_X^{EM} = 64/9, \quad b_B^c = b_X^c = 2/3.$$

$$z_f \equiv \frac{\partial}{\partial \log v} \left(\sum_i \log m_{f,i}^2(v) \right),$$

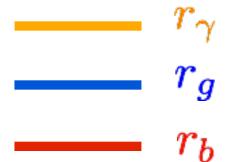
$$z_B \simeq -4 \frac{Y_4 Y_5}{M_1 M_2} \qquad z_X \simeq -4 \frac{Y_6 Y_7}{M_1 M_3}$$

$$r_{\gamma} \simeq \left| 1 + 0.13 \left(\frac{Y_4 Y_5}{M_1 M_2} + 16 \frac{Y_6 Y_7}{M_1 M_3} \right) \right|^2$$
 , $r_g \simeq \left| 1 - 2.1 \left(\frac{Y_4 Y_5}{M_1 M_2} + \frac{Y_6 Y_7}{M_1 M_3} \right) \right|^2$



$$Y_4 = Y_5 = Y_B$$

 $Y_6 = Y_7 = Y_X$
 $M_{1,2,3} = 800 \text{ GeV}$



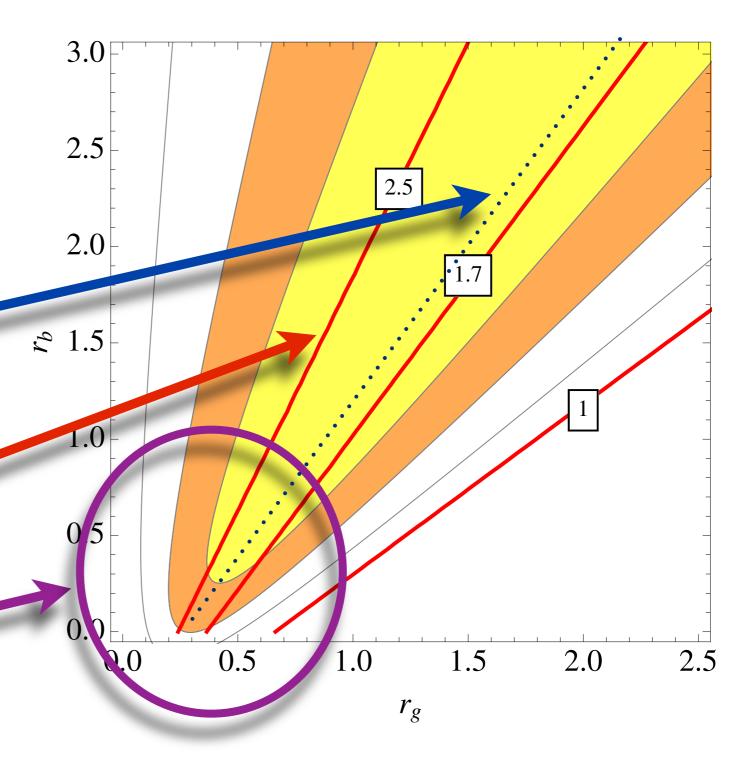
What does the signal strength data say?

$$\mu_{\gamma\gamma} \simeq rac{r_g r_{\gamma}}{1 + \mathrm{Br}_b(r_b - 1) + \mathrm{Br}_g(r_g - 1)},$$
 $\mu_{VV} \simeq rac{r_g}{1 + \mathrm{Br}_b(r_b - 1) + \mathrm{Br}_g(r_g - 1)},$
 $\mu_{b\bar{b}} \simeq rac{r_b}{1 + \mathrm{Br}_b(r_b - 1) + \mathrm{Br}_g(r_g - 1)}$

Shallow direction in $r_g - r_b$ plane

Marginalize over r_{γ}

The model lives in this region



Direct searches for Heavy Quarks

- Signatures similar to minimal (3,2,-5/6) model [Kumar, Shepard, Tait, Vega-Morales '10]
- Most robust limit comes from top prime searches

CMS search in dilepton channel [CMS-EXO-11-050]

$$pp \to t'\bar{t}' \to (W^+b)(W^-\bar{b}) \to \ell^+\ell^-\nu\nu\bar{b}\bar{b}$$

Bounds masses heavier than $m_{t'} > 557~{
m GeV}$

• These bounds apply since X decays via $X \to bW^-$

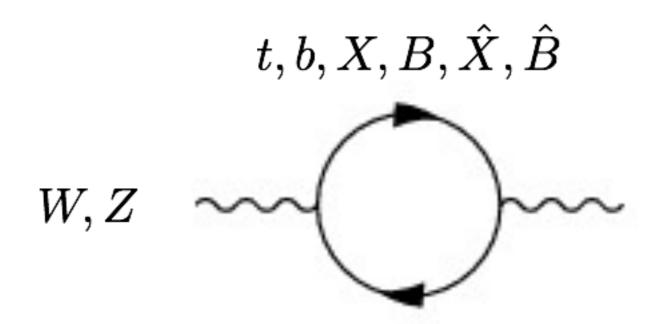
Other possible decay mode $X \to BW$ requires $m_X > m_B + m_W$, not favored by Higgs data (see shortly)

Also bounds exist from bottom prime searches:

$$pp \to b'\bar{b}' \to W^-tW^+\bar{t} \to 4W2b \to 3\ell + b \text{ or SS } \ell + b$$

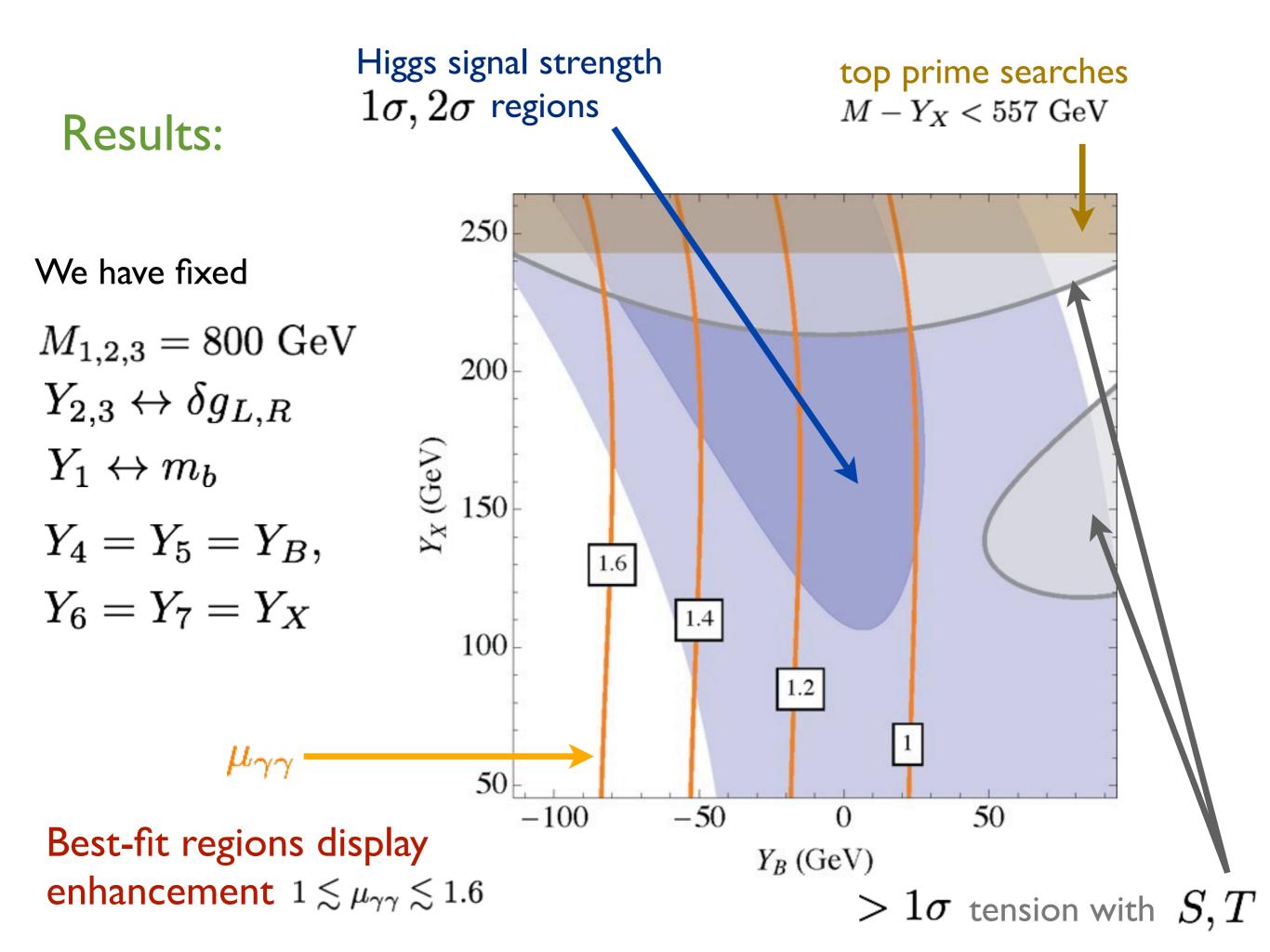
Bounds masses heavier than $m_{b'} > 611 \text{ GeV}$

[CMS-EXO-11-036]



- Contribution from new mirror quarks
- ullet $War{t}b,Zar{b}b$ vertices modified include t,b and subtract off SM
- ullet Restrict to 1σ regions determined by fit (including $\delta g_{L,R}$)

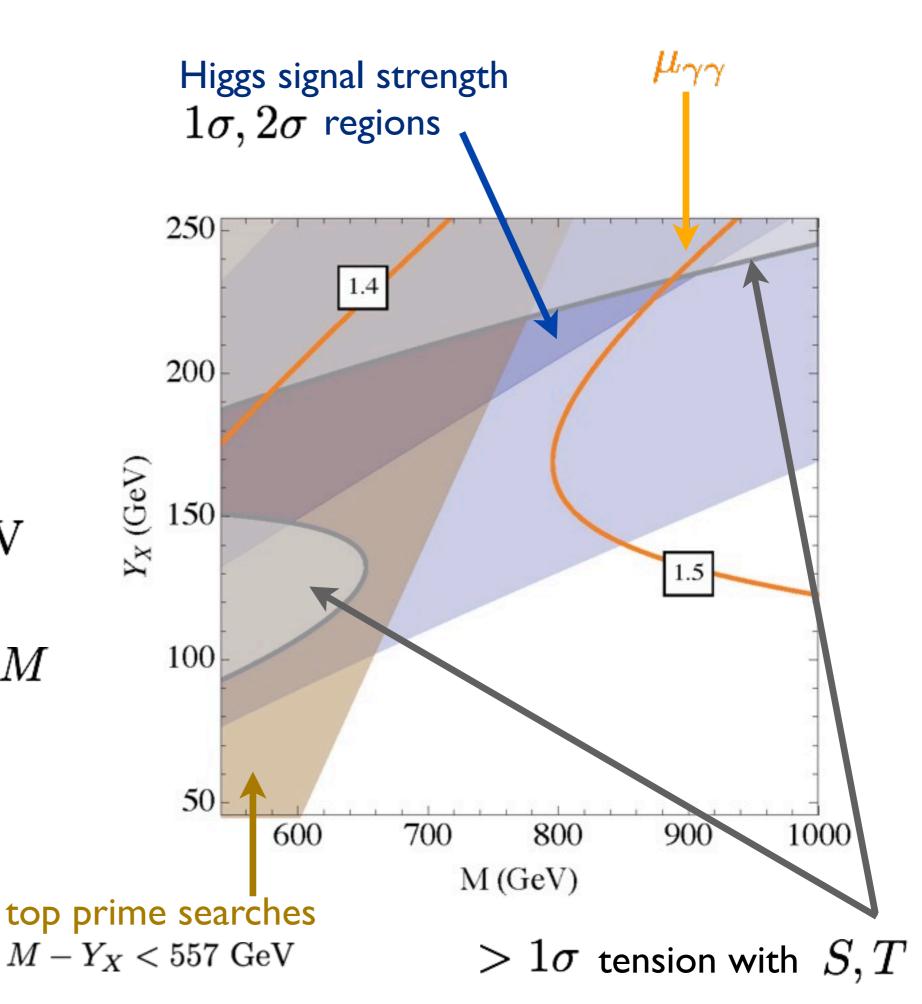
$$S = -0.02 \pm 0.09$$
, $T = 0.03 \pm 0.08$, $\rho \sim 0.90$



Results:

We have fixed

$$Y_{2,3} \leftrightarrow \delta g_{L,R}$$
 $Y_1 \leftrightarrow m_b$
 $Y_4 = Y_5 = -65 \text{ GeV}$
 $Y_6 = Y_7 = Y_X$
 $M_1 = M_2 = M_3 = M$



Caveat: Vacuum stability

As emphasized recently in several works, new fermions with O(I) Yukawa's drive Higgs quartic negative at low scale

Jogelkar, Schwaller, Wagner `12 Arkani-Hamed, Blum, D'Agnolo, Fan `12 Reece `12

In our model,

$$16\pi^2\beta_{\lambda} \simeq 24\lambda^2 + 12\lambda(y_t^2 + y_4^2 + y_5^2 + y_6^2 + y_7^2) - 6(y_t^4 + y_4^4 + y_5^4 + y_6^4 + y_7^4)$$

e.g.
$$y_4 = y_5 = 0, y_6 = y_7 = 1$$
; VL threshold $M = 800 \text{ GeV}$

$$\lambda = 0$$
 at $Q = 2 \text{ TeV}$

- Model requires a UV completion to stabilize vacuum...
- Obvious candidate is a SUSY version (beyond scope here)

Outlook:

- 125 GeV Higgs discovered as suggested by EW data
- Slight enhancement in $\mu_{\gamma\gamma}$, need more data
- Two discrepancies in EW data: A_{FB}^{b} (2.6 σ), R_{b} (2.4 σ)
- Beautiful Mirrors shift $Z \overline{b}_R b_R$ by b-B mixing
- Mirror quarks can cause deviations in Higgs properties
- Model is testable at LHC via search for mirror quarks

Backup

Ingredients going into the electroweak fit:

Observables

$$m_{Z}, \; \Gamma_{Z}, \; \sigma_{\mathrm{had}}^{0}, \; R_{\ell}, \; R_{c}, \; R_{b}, \ A_{FB}^{\ell}, \; A_{\ell}, \; A_{c}, \; A_{b}, \; A_{FB}^{c}, \; A_{FB}^{b}, \; \sin^{2}\theta_{\mathrm{eff}}, \ m_{W}, \; \Gamma_{W}, \; m_{t}, \; \Delta\alpha_{\mathrm{had}}^{(5)}, \; m_{h}$$

Vary SM + NP parameters in fit

$$m_H, m_Z, m_t, \Delta \alpha_{\rm had}^{(5)}, \alpha_s,$$

 $S, T, \delta g_{Lb}, \delta g_{Rb}$

• Theory predictions taken from various numerical parameterizations in literature...

2. A_{FB}^b , R_b due to systematic effect

EW data alone (w/o LHC Higgs mass measurement)

SM w/o
$$A_{FB}^b, R_b$$
 :
$$p = 0.92$$

$$m_h = 70 \pm 30 \; \mathrm{GeV}$$

SM w/o
$$A_{FB}^b, R_b$$
 $p=0.90$ $S=-0.08\pm0.10$ $S=-0.08\pm0.10$ $T=0.0\pm0.08$

- Slight tension between indirect determination of Higgs mass (70 GeV) and 125 GeV
- New contribution to oblique parameters?

2. A_{FB}^b , R_b due to systematic effect

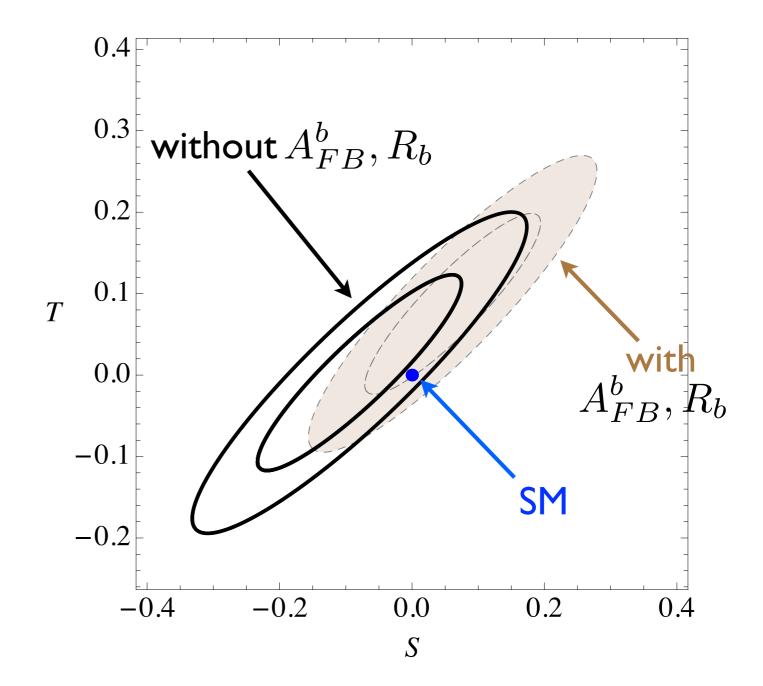
Including LHC Higgs mass measurement:

SM w/o
$$A_{FB}^b, R_b$$
: $p=0.67$ $m_h=125.7~{
m GeV}$

SM w/o A_{FB}^b, R_b $p=0.78$ $S=-0.08\pm0.10$ $T=0.0\pm0.08$

- Marginal improvement with oblique parameters.
- No strong argument for new physics to pull up Higgs mass

S-T fit without A_{FB}^b,R_b



Electroweak fit (w/o A_{FB}^b, R_b) marginally improved with non-zero S,T